

Dynamics of beam structures: From localized to distributed nonlinearities

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XXXII Cycle

Localized nonlinearity: dynamics of overhead contact lines

Modelling of overhead contact lines

- Certified nonlinear software (CEI EN50318): CateWay.

- Nonlinearity in:

→ Slackening of the droppers

→ Loss of contact

- How to properly tune the FEM parameters?

→ Comparison between FE models and a distributed parameter model.

■ S. Sorrentino, D. Anastasio, A. Fasana, S. Marchesiello, *Distributed parameters and finite element models for wave propagation in railway contact lines*, J. Sound Vib. 410 (2017) 1-18.

- How to define the damping distribution?

→ Study on non-proportional damping distributions: contact wire with a lumped damper.

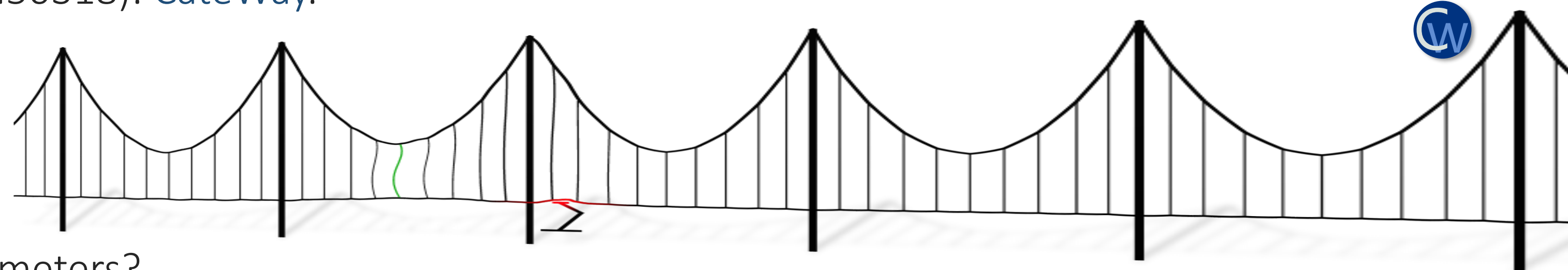
→ Experimental measurements on railway contact wire and comparison with model predictions.

■ D. Anastasio, A. Fasana, L. Garibaldi, S. Marchesiello, *Analytical investigation of railway overhead contact wire dynamics and comparison with experimental results*, Mech. Syst. Signal Process. 116 (2019) 277–292.

- How to improve the performance of OCLs?

→ Design of nonlinear damping systems for OCLs, based on a negative stiffness absorber.

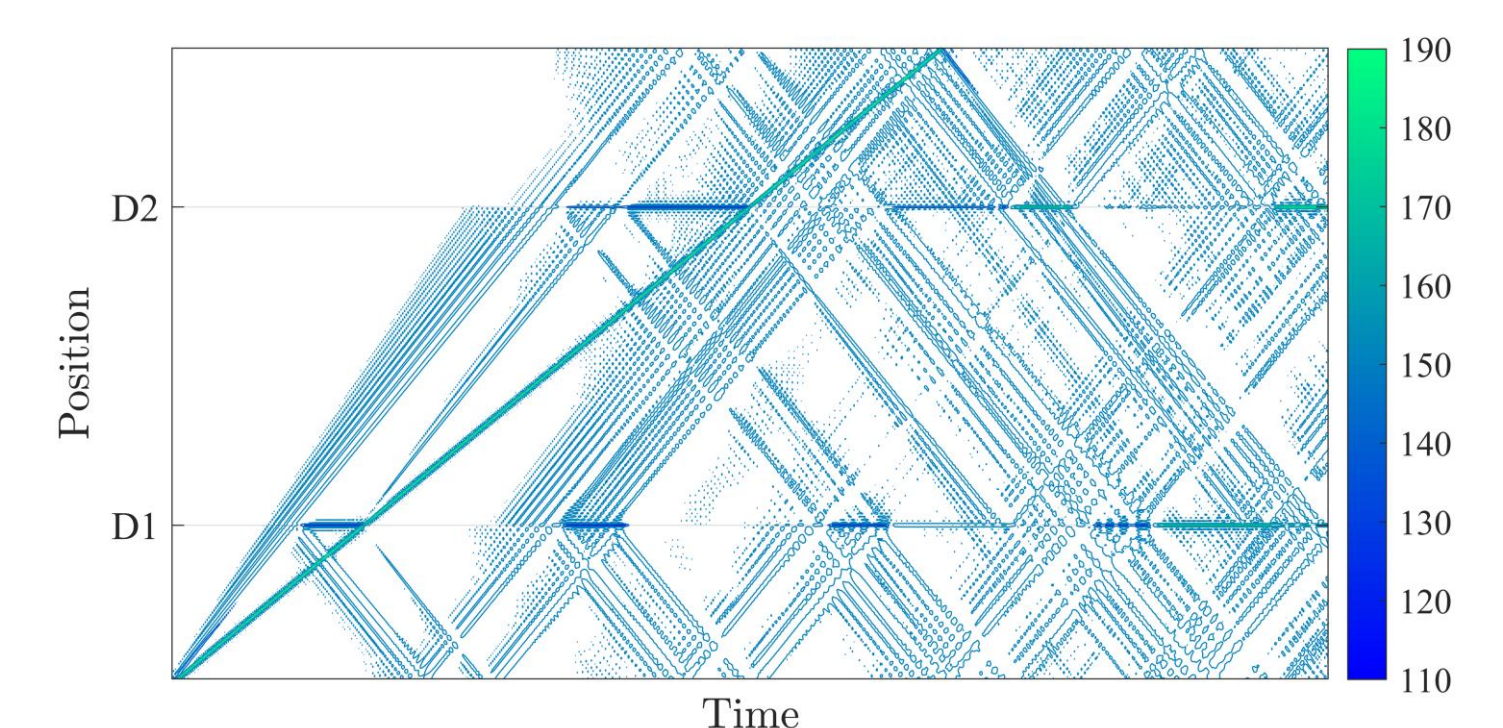
■ S. Marchesiello, D. Anastasio, L. Garibaldi, A. Fasana, International patent No. WO2018020397A8 (2018).



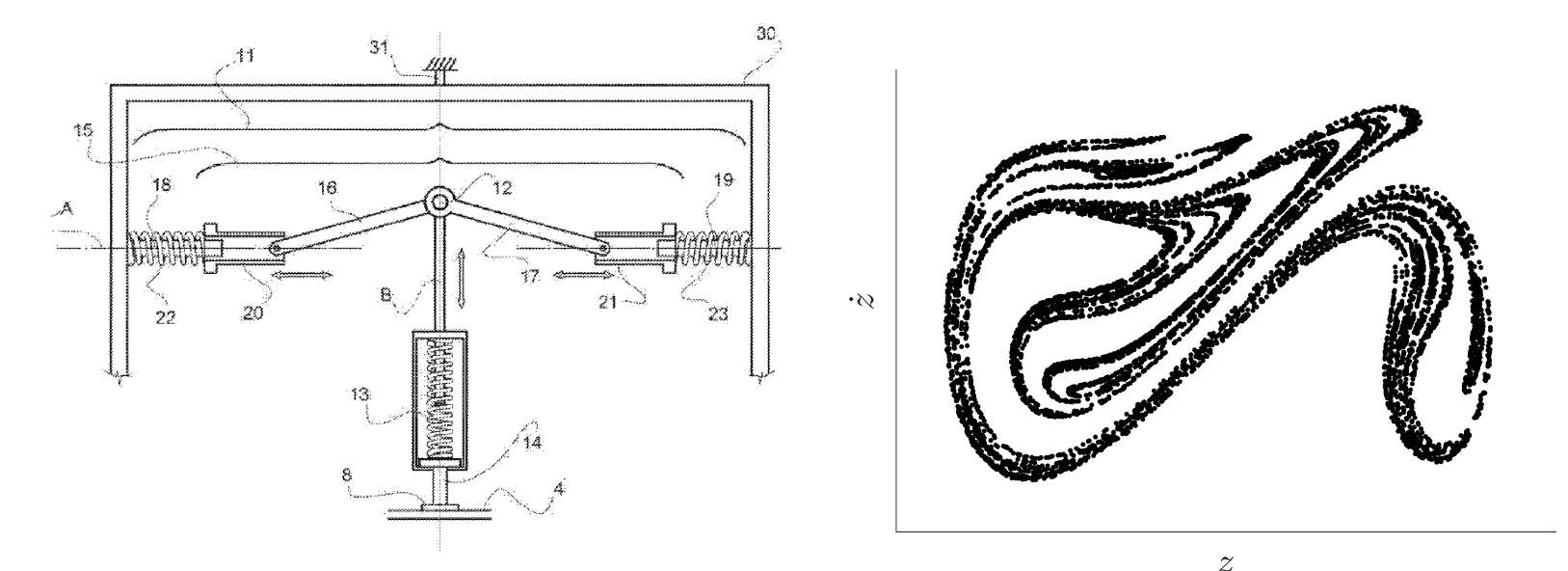
Photos of the experimental setup



Stress level (MPa) in the contact wire



Damper for OCLs and Poincaré map of the frame



Distributed nonlinearity: beam under large oscillations

Reduced Order Model (ROM)

- Constitutive nonlinear equation:

$$\mu \frac{\partial^2 y}{\partial t^2} + EI \frac{\partial^4 y}{\partial x^4} - \frac{EA}{2L} \left(\int_0^L \left(\frac{\partial y}{\partial x} \right)^2 dx \right) \frac{\partial^2 y}{\partial x^2} = f(x, t)$$

- A ROM is built starting from the linear modeshapes ϕ_j

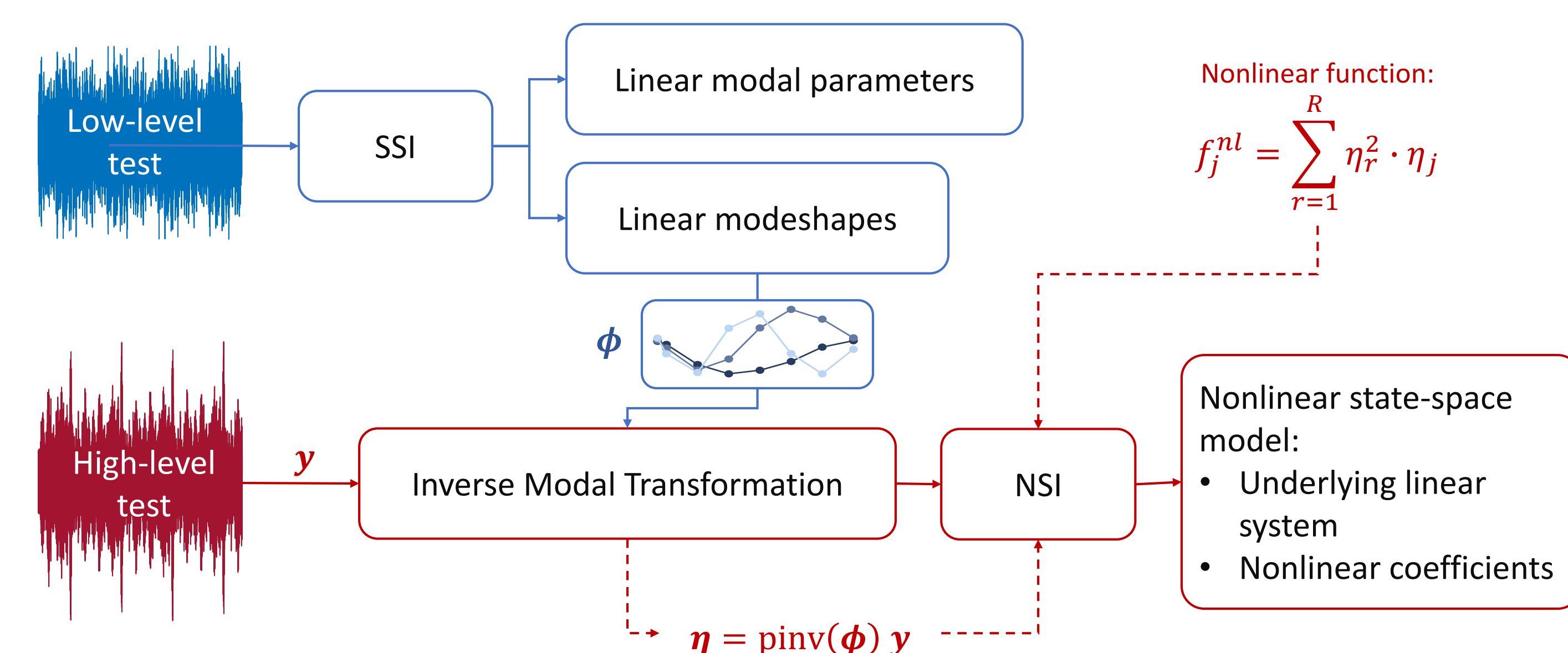
- A set of N nonlinear equations in the modal domain is obtained considering N modes:

$$m_j \ddot{\eta}_j + k_j \eta_j - \frac{EA}{2L} \sum_{r=1}^R (c_{1,r}^{nl} \eta_r^2) c_{2,j}^{nl} \eta_j = Q_j, \quad j = 1, \dots, N, \quad R \leq N$$

- The nonlinear term shows an odd nonlinearity coupling different modes.

Nonlinear System Identification

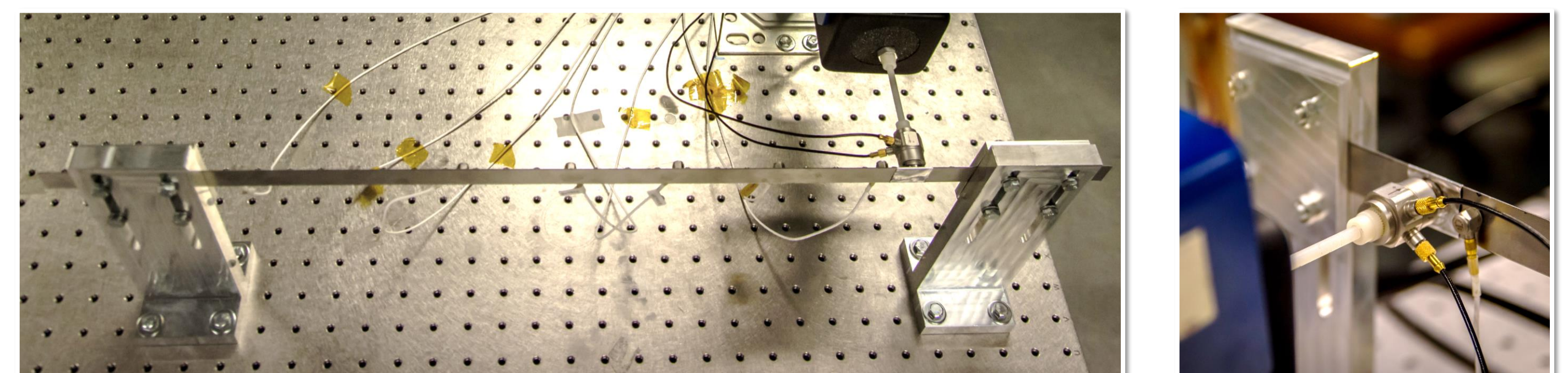
- NSI (Nonlinear Subspace Identification) method is used to extract the modal parameters of the underlying linear system, and to identify the nonlinear coefficients.
- The identification is performed in the (extended) modal domain.



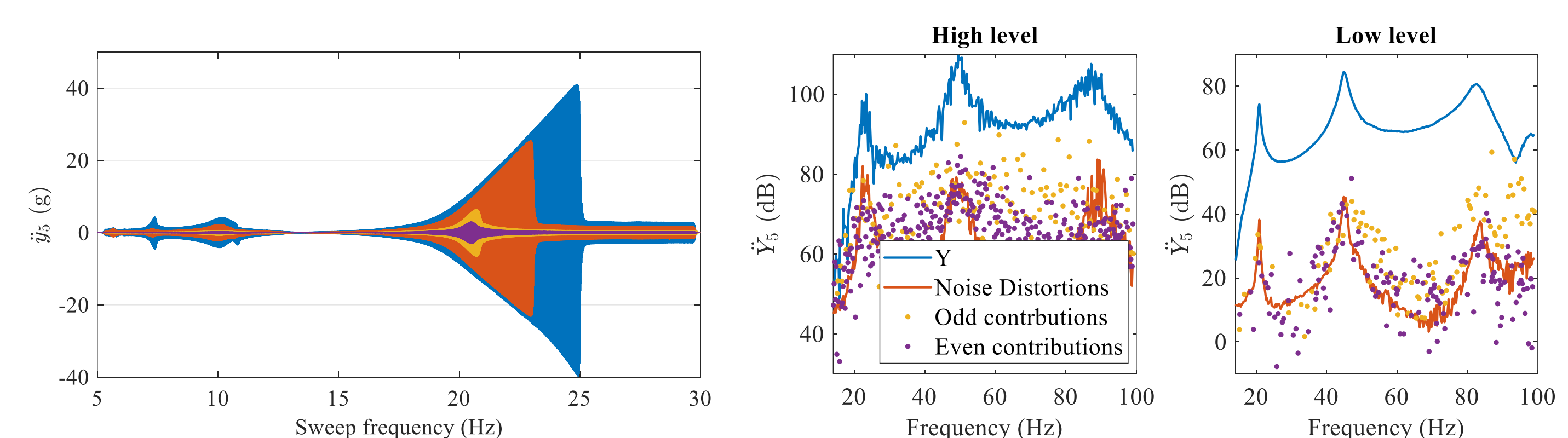
Experimental tests

- Tests are conducted at University of Liège, Space Structures and Systems Lab.
- A very thin alloy beam is driven through large oscillations, showing a distinctive distributed nonlinear behavior.
- NSI is applied to identify the nonlinearity.
- Even nonlinear contributions are included as well, to account for asymmetries in the structure.

Photos of the experimental setup



Sweep tests and nonlinearity detection for different amplitudes: from linear to nonlinear



Results of the identification

